



# Problem of the Week

## Problem C and Solution

### Slightly Irregular

#### Problem

In the following slightly irregular shape,  $AB = 50$  cm,  $CD = 15$  cm,  $EF = 30$  cm, the area of the shaded triangle,  $\triangle DEF$ , is  $210$  cm<sup>2</sup>; and the area of the entire figure,  $ABCDE$ , is  $1000$  cm<sup>2</sup>. Determine the length of  $AE$ .

#### Solution

The first task is to mark the given information on the diagram. This has been completed on the diagram to the right.

To find the area of a triangle, multiply the base length by the height and divide by 2. In  $\triangle DEF$ , the base,  $EF$ , has length 30 cm. The height of  $\triangle DEF$  is the perpendicular distance from  $EF$  (extended) to vertex  $D$ , namely  $GD$ . The area is given. So

$$\begin{aligned} \text{Area } \triangle DEF &= \frac{30 \times GD}{2} \\ 210 &= 15 \times GD \\ 14 &= GD \end{aligned}$$

We know that  $EH = AB = 50$ ,  $GH = DC = 15$ , and  $EH = EF + FG + GH$ . It follows that  $50 = 30 + FG + 15$  and  $FG = 5$  cm.

Now we can relate the total area to the areas contained inside.

$$\begin{aligned} \text{Area } ABCDE &= \text{Area } ABHE + \text{Area } CDGH + \text{Area } \triangle DFG + \text{Area } \triangle DEF \\ 1000 &= AB \times AE + DG \times DC + \frac{FG \times GD}{2} + 210 \\ 1000 &= 50 \times AE + 14 \times 15 + \frac{5 \times 14}{2} + 210 \\ 1000 &= 50 \times AE + 210 + 35 + 210 \\ 1000 &= 50 \times AE + 455 \\ 1000 - 455 &= 50 \times AE \\ 545 &= 50 \times AE \\ \frac{545}{50} &= AE \end{aligned}$$

$\therefore AE = 10.9$  cm.

