

Problem of the Week Problem C That's Odd

$$1 = 1^{2}$$

$$1 + 3 = 4 = 2^{2}$$

$$1 + 3 + 5 = 9 = 3^{2}$$

$$1 + 3 + 5 + 7 = 16 = 4^{2}$$

Did you know that the sum of the first n positive odd integers is n^2 ? The diagram above illustrates the first four possible sums. The sum of the first five positive odd integers would be 5^2 or 25. We can easily check to see that 1 + 3 + 5 + 7 + 9 = 25.

When adding the first a positive odd integers to the first b positive odd integers, the sum is 180. If p is the largest odd number in the first set of numbers and q is the largest odd number in the second set of numbers, then determine the sum p+q.

